Date: _____

Rational and Irrational Number Notes

8.NS.A.1 Know that numbers that are not rational are called irrational. Understand informally that every number has a decimal expansion; for rational numbers show that the decimal expansion repeats eventually, and convert a decimal expansion, which repeats eventually into a rational number.

Rational Number -

Irrational Number -

Place the numbers in the correct place in the Venn diagram.



Reflect:

1) Consider the decimal 0.20200200020000200002... Do you think this decimal represents a rational number? Why or why not?

2) Do you think a negative sign affects whether or not a number is a rational number? Use $-\frac{4}{5}$ as an example. Why or why not?

3) Do you think a mixed number is a rational number? Explain.

Long Division Time:

Write the following fractions as decimals:

1.
$$\frac{5}{16}$$
 2. $\frac{2}{11}$

Question...Do you think that decimals that have repeating patterns always have the same number of digits in their pattern? Explain.

Writing Mixed Numbers as Decimals

Ms. Haley bought $3\frac{1}{8}$ yards of material to make an outfit for her daughter. Write $3\frac{1}{8}$ as a decimal.

Step 1: Turn to improper fraction $3\frac{1}{8}$

Step 2: Divide numerator by denominator

Practice:

A. Abbey made
$$4\frac{1}{5}$$
 quarts of Kool-Aid. Write $4\frac{1}{5}$ as a decimal.

B. Josh bought a cantaloupe that weighed $6\frac{2}{3}$ pounds. Write $6\frac{2}{3}$ as a decimal.

Write each of the following fractions or improper fractions as decimals.

C. $-\frac{7}{20}$ D. $\frac{23}{4}$ E. $\frac{58}{8}$

Write the following as fractions/mixed numbers in lowest terms.

F. -0.4 *G*. 0.05 H. 0.75 I. -1.45 J. 4.35

K. Write each number in its appropriate box to show its placement along the number line.



Repeating Decimal as a Fraction

Consider the following:

A.
$$x = 0.\overline{3}$$
(10) $x = 10(0.\overline{3})$ $10x = 3.\overline{3}$ Because $x = 0.\overline{3}$ you can subtract x from one side $\frac{-x - 0.\overline{3}}{9x = 3}$ and $0.\overline{3}$ from the other $9x = 3$ Now solve the equation for x.

B.
$$x = 0.\overline{37}$$
 (100) $x = 100(0.\overline{37})$
 $100x = 37.\overline{37}$ Because $x = 0.\overline{37}$ you can subtract x from one
 $\frac{-x - 0.\overline{37}}{99x = 37}$ side and $0.\overline{37}$ from the other
 $99x = 37$ Now solve the equation for x .

C.
$$x = 0.\overline{512}$$
(1000)x = 1000($0.\overline{512}$) $1000x = 512.\overline{512}$ Because $x = 0.\overline{512}$ you can subtract x from $-x - 0.\overline{512}$ one side and $0.\overline{512}$ from the other. $999x = 512$ Now solve the equation for x.

What pattern do you see?

Do you think it will work with all repeating decimals?

What is the fraction for: